

Interest Rate *Floor CMS - CMS spread*

1 Introduction

An Interest Rate *Floor* is (generally) an O.T.C. derivative contract based on a series of European interest rate put options. This interest rate sensitive instrument protects the floor buyer from losses resulting from a decrease in interest rates. The floor seller compensates the buyer with a payoff when the reference interest rate falls below the floor strike rate. In details the underlying of this Interest Rate *Floor* is a CMS rate or the differential between two CMS rates.

Interest Rate <i>Floor CMS - CMS spread</i>	
Principal	100 <i>bullet</i>
Trade Date	23/03/2010
Effective Date	25/03/2010
Termination Date	25/03/2015
Payment Frequency	<i>Quarterly</i>
Payoff	
From Effective to Termination date	$\max[1\% - (30\text{-Year CMS} - 2\text{-Year CMS}); 0\%]$
Conventions	
Reset dates	<i>Advance, 2 days before</i>
Day Count Fraction	<i>Act/360 (Adjusted)</i>

Table 1: *Example of an Interest Rate Floor CMS - CMS spread template.*

2 Template implementation

This section describes the constants, symbols and functions we used for the implementation of the template:

Interest Rate <i>Floor CMS - CMS spread</i> on <i>Fairmat</i>	
Principal	N
Trade Date	Trading date (simulation start date)
Effective Date	Contract initial date
Termination Date	Pd [end]
Payment Frequency	matRate -Year (exchange per year)
Payoff	
From 1 to <i>length(@Pd)</i> $\max[\text{levStk}*\text{stk} - (\text{levCMS1}*\text{matCMS1}\text{-Year CMS} - \text{levCMS2}*\text{matCMS2}\text{-Year CMS}) ; 0\%]$	
Conventions	
Reset dates	Advance , rday days before
Day Count Fraction	Dur

Table 2: *Example of Interest Rate Floor CMS - CMS spread template described through Fairmat objects.*

The variables of Interest Rate *Floor CMS - CMS spread* template loaded on “Parameters & Functions” can be classified into three categories:

N	pdu
100.00	25/06/2010
100.00	25/09/2010
100.00	25/12/2010
100.00	25/03/2011
100.00	25/06/2011
100.00	25/09/2011
100.00	25/12/2011
100.00	25/03/2012
100.00	25/06/2012
100.00	25/09/2012
100.00	25/12/2012
100.00	25/03/2013
100.00	25/06/2013
100.00	25/09/2013
100.00	25/12/2013
100.00	25/03/2014
100.00	25/06/2014
100.00	25/09/2014
100.00	25/12/2014
100.00	25/03/2015

Table 3: *Input (Vectors) of Interest Rate Floor CMS - CMS spread template loaded on “Parameters & Functions” Fairmat environment.*

1. Contract specific parameters:

- **N**: principal, bullet or amortizing (see Table 3);
- **pdu**: payment date (unadjusted), used for auxiliary item **Pd** (see Table 3);

- **matCMS1**: time horizon of CMS rate n.1, expressed in years;
- **levCMS1**: leverage on CMS rate n.1;
- **tenor1**: payment frequency of CMS rate n.1 (exchange per year);
- **matCMS2**: time horizon of CMS rate n.2, expressed in years. It is used only with *CMS spread* floor;
- **levCMS2**: leverage on CMS rate n.2. It is used only with *CMS spread* floor;
- **tenor2**: payment frequency of CMS rate n.2 (exchange per year). It is used only with *CMS spread* floor;
- **levStk**: leverage on strike (**stk**) rate;
- **stk**: strike rate;
- **rday**: number of days before *Initial (Advance)* / *Ending (Arrears)* period;

2. *Market* data:

- **zr**: zero rate (derived from *spot* rate);

3. *Auxiliary* and *Instrumental* variables: the following elements are other objects and functions that aren't input – they are derived from or depend on *Contract specific* data or *Market* data inputs – but they are useful for use within “*Option Map*” environment.

- **FloorletSpread**: analytic function of a *floorlet* payoff with underlying an unique CMS rate¹ or a differential CMS rates;
- **Pd**: date's vector transformation from **pdu** vector (see Table 3);
- **Rd**: date's vector transformation from **pdu** vector (see Table 3) using **rday** constant;
- **Dur**: date's vector difference transformation from **pdu** vector (see Table 3);

¹In this case **matCMS2**, **tenor2** and **levCMS2** aren't used.