

Interest Rate *Collar CMS - CMS spread*

1 Introduction

An Interest Rate *Collar* is an instrument created to guarantee that the interest rate on the underlying floating rate always lies between a ceiling and a floor. It is a combination of a long position in a cap and a short position in a floor. In details the underlying of this Interest Rate *Cap* is a CMS rate or the differential between two CMS rates.

Interest Rate <i>Collar CMS - CMS spread</i>		
Principal		100 <i>bullet</i>
Trade Date		28/06/2004
Effective Date		30/06/2004
Termination Date		30/06/2014
Payment Frequency		<i>Quarterly</i>
Payoff		
From the First to the Tenth year	If $(30\text{-Year CMS} - 2\text{-Year CMS}) \leq 0.25\%$	0.25% + 1.00%
	If $0.25\% < (30\text{-Year CMS} - 2\text{-Year CMS}) \leq 3.00\%$	—
	If $(30\text{-Year CMS} - 2\text{-Year CMS}) > 3.00\%$	3.00% + 0.20%
Conventions		
Reset dates		<i>Arrears, 2 days before</i>
Day Count Fraction		<i>Act/360 (Adjusted)</i>

Table 1: *Example of an Interest Rate Collar CMS - CMS spread template.*

2 Template implementation

This section describes the constants, symbols and functions we used for the implementation of the template:

Interest Rate Collar CMS - CMS spread on <i>Fairmat</i>	
Principal	N
Trade Date	Trading date (simulation start date)
Effective Date	Contract initial date
Termination Date	$Pd[end]$
Payment Frequency	frequency of Pd
Payoff	
From 1 to length(@Pd)	$\begin{aligned} & \text{If } (levCMS1 * matCMS1 - Year CMS - levCMS2 * matCMS2 - Year CMS) \leq (levStkfloor * Stklow) + sprlow \\ & \text{If } (levStkfloor * Stklow) < (levCMS1 * matCMS1 - Year CMS - levCMS2 * matCMS2 - Year CMS) \leq (levStkcap * Stkhigh) \\ & \text{If } (levCMS1 * matCMS1 - Year CMS - levCMS2 * matCMS2 - Year CMS) > (levStkcap * Stkhigh) + sprhigh \end{aligned}$
Conventions	
Reset dates	Arrears, rdays days before
Day Count Fraction	Dur

Table 2: Example of Interest Rate Collar CMS - CMS spread template described through *Fairmat* objects.



The variables of Interest Rate *Collar* template loaded on “*Parameters & Functions*” can be classified into three categories:

pdu	N	Stklow	Stkhigh	sprlow	sprhigh
30/12/2004	100	0.25%	3.00%	1.00%	0.20%
30/06/2005	100	0.25%	3.00%	1.00%	0.20%
30/12/2005	100	0.25%	3.00%	1.00%	0.20%
30/06/2006	100	0.25%	3.00%	1.00%	0.20%
30/12/2006	100	0.25%	3.00%	1.00%	0.20%
30/06/2007	100	0.25%	3.00%	1.00%	0.20%
30/12/2007	100	0.25%	3.00%	1.00%	0.20%
30/06/2008	100	0.25%	3.00%	1.00%	0.20%
30/12/2008	100	0.25%	3.00%	1.00%	0.20%
30/06/2009	100	0.25%	3.00%	1.00%	0.20%
30/12/2009	100	0.25%	3.00%	1.00%	0.20%
30/06/2010	100	0.25%	3.00%	1.00%	0.20%
30/12/2010	100	0.25%	3.00%	1.00%	0.20%
30/06/2011	100	0.25%	3.00%	1.00%	0.20%
30/12/2011	100	0.25%	3.00%	1.00%	0.20%
30/06/2012	100	0.25%	3.00%	1.00%	0.20%
30/12/2012	100	0.25%	3.00%	1.00%	0.20%
30/06/2013	100	0.25%	3.00%	1.00%	0.20%
30/12/2013	100	0.25%	3.00%	1.00%	0.20%
30/06/2014	100	0.25%	3.00%	1.00%	0.20%

Table 3: *Input (Vectors) of Interest Rate Collar CMS - CMS spread template loaded on “Parameters & Functions” Fairmat environment.*

1. *Contract specific* parameters:

- **N**: principal, bullet or amortizing (see Table 3);
- **pdu**: payment date (unadjusted), used for auxiliary item **Pd** (see Table 3);
- **Stklow**: strike rate on floor (see Table 3);
- **Stkhigh**: strike rate on cap (see Table 3);
- **sprlow**: spread added to floor strike rate (see Table 3);
- **sprhigh**: spread added to cap strike rate (see Table 3);
- **levStkfloor**: leverage on strike (**Stklow**) rate;
- **levStkcap**: leverage on strike (**Stkhigh**) rate;
- **rday**: number of days before *Initial (Advance) / Ending (Arrears)* period;
- **matCMS1**: time horizon of CMS rate n.1, expressed in years;
- **matCMS2**: time horizon of CMS rate n.2, expressed in years;
- **tenor1**: payment frequency of CMS rate n.1 (exchange per year);
- **tenor2**: payment frequency of CMS rate n.2 (exchange per year);
- **levCMS1**: leverage on CMS rate n.1;
- **levCMS2**: leverage on CMS rate n.2;
- **rday**: number of days before *Initial (Advance) / Ending (Arrears)* period;

2. *Market* data:

- **zr**: zero rate (derived from *spot* rate);
3. *Auxiliary* and *Instrumental* variables: the following elements are other objects and functions that aren't input – they are derived from or depend on *Contract specific* data or *Market* data inputs – but they are useful for use within “*Option Map*” environment.
- **D**: computes the CMS spread (with leverage on CMS rates);
 - **Collar**: analytic function of a *+caplet - floorlet* payoff. It uses the **D** function;
 - **Caplet**: analytic function of a *caplet* payoff;
 - **Floorlet**: analytic function of a *floorlet* payoff;
 - **Pd**: date's vector transformation from **pdu** vector (see Table 3);
 - **Rd**: date's vector transformation from **pdu** vector (see Table 3) using **rday** constant;
 - **Dur**: date's vector difference transformation from **pdu** vector (see Table 3).